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Generation of One-Group Cross Sections for coupled MC codes

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☐ Introduction

- ☐ Depletion problem description

☐ Multi-group approach

- ☐ Choosing the number of groups
- ☐ Generating self shielded cross sections
- ☐ Calculating background cross section

☐ Results

- ☐ Number of groups vs. CPU time

☐ Summary and conclusions

Depletion problem



- Solve Bateman eq. for each nuclide in each burnable zone:

$$\underbrace{\frac{dN_j(t)}{dt}}_{\text{Rate of amount change of nuclide i}} = \underbrace{-\lambda_j N_j(t)}_{\text{Disappearance due to decay}} - \underbrace{\phi \sigma_j N_j(t)}_{\text{Disappearance due to neutron absorption}} + \sum_{k=1}^{k=n} \underbrace{\lambda_k BR_{k \rightarrow j} N_k(t)}_{\text{Buildup due to decay of other nuclides}} + \underbrace{\phi (\sigma_{k \rightarrow j} N_k(t))}_{\text{Buildup due to absorption in other nuclides}}$$

- Required data:

- Decay constants \Rightarrow available directly from ENDF
- Fission product yields \Rightarrow available directly from ENDF
- One-group cross sections \Rightarrow MC transport solution
- Fluxes \Rightarrow MC transport solution



❑ **Direct tally** method

- MC transport to obtain 1G reaction rates:
 - For every reaction type;
 - In every isotope;

❑ **Multi-group (MG)** method

- MC transport to obtain fine spectrum (>10K groups)
- External collapsing procedure into 1G
 - Requires separate lib of pre-generated MG cross-sections for each isotope and reaction type

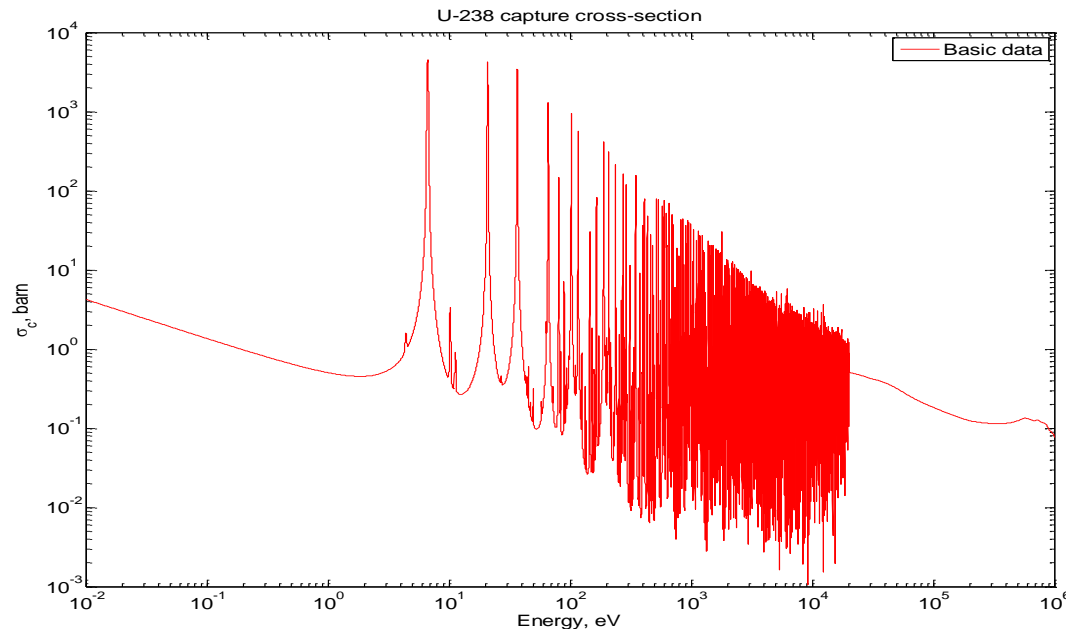
❑ **Main trade-offs**

- Direct tally ⇒ requires more CPU time (up to ×30)
- MG ⇒ requires more data storage space

Preparation of MG data sets (1)



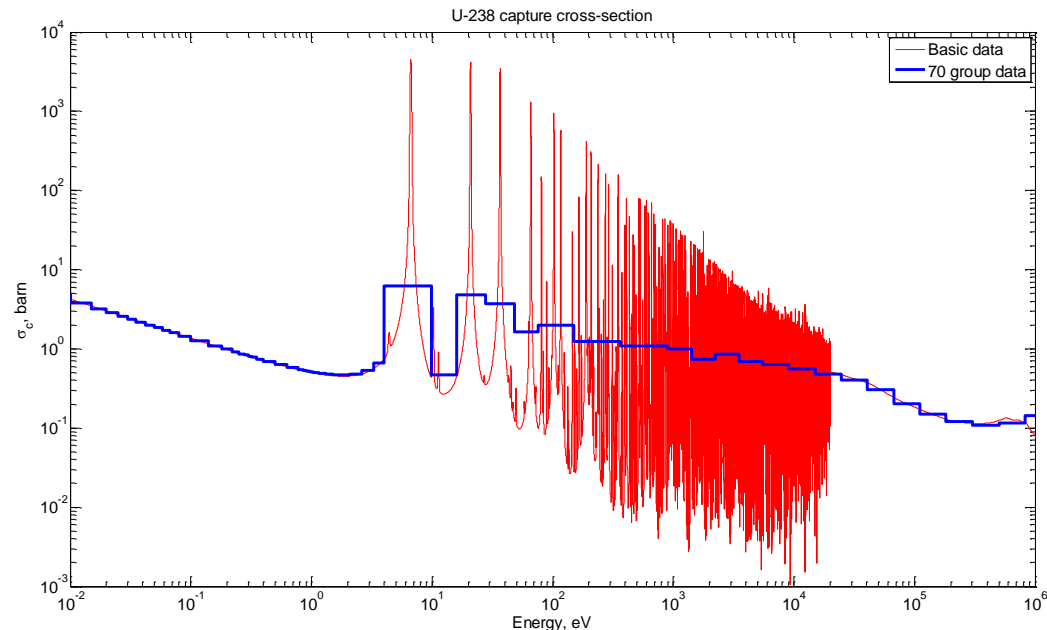
- Basic data libraries
 - Reaction cross sections: (n,γ) , (n,f) , (n,xn) , etc
 - Cover entire neutron energy range (up to 25 MeV)
 - Examples:
 - Joint European Data Files (JEFF)
 - Evaluated Nuclear Data Files (ENDF)



Preparation of MG data sets (2)



- ❑ Routine reactor calculation practices:
 - Basic point wise data is not used directly
 - Use pre-generated microscopic cross-sections in limited no. of groups
 - *Typical energy range covered: 0.0001 eV – 25 MeV*
 - **NJOY** is used to generate MG XS in few groups
 - *Group XS become spectrum dependent*
 - *Require tabulation against T and Bondarenko “background”*





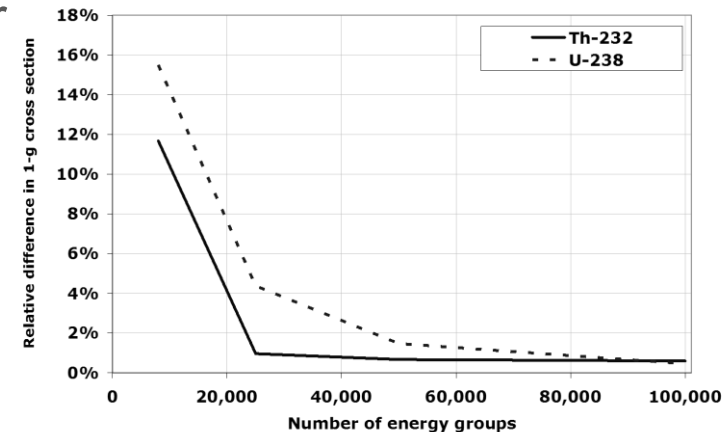
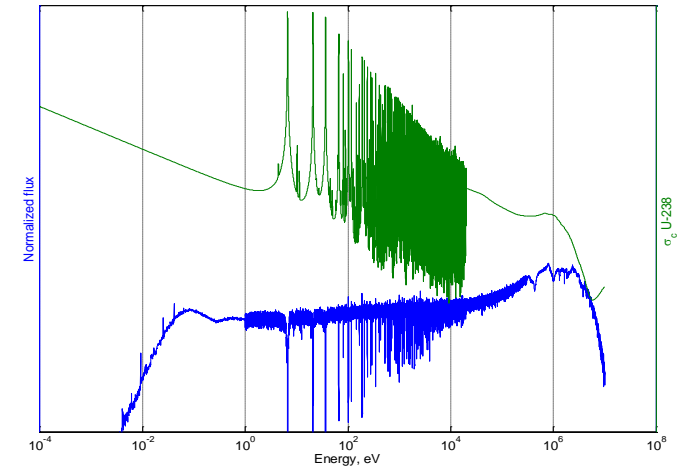
□ Presumably, if $NG \rightarrow \infty \Rightarrow$ infinite dilution XS can be used

■ Preserving the reaction rates:

$$\Rightarrow \bar{\sigma} = \frac{\int \sigma(E) \varphi(E)}{\int \varphi(E)} \Rightarrow \bar{\sigma} = \frac{\sum \sigma_i \varphi_i}{\sum \varphi_i}$$

□ Proved to be not true

- Probabilistic treatment of unresolved res.
- Even with $NG \rightarrow \infty$, $\sim 1\%$ systematic error
- **Solution:**
 - tabulate against background XS
- Background XS is not easy to obtain





- ❑ **Simplified tabulation against σ_0** (Fridman et al., 2008)
 - Generate fine group XS for multiple values of σ_0
 - Tabulation is used only in the resonance region
 - Calculate energy and spatial components of σ_0
 - Use potential scattering XS data from ENDF
 - Ask user to provide basic fuel geometry (e.g. chord length)
 - Interpolate between σ_0 to obtain “shielded” in each group
 - The approach was proven to fix the systematic error problem

Simplified σ_0 model ($a = \gamma = 1$)



- The approach simplifies basic lattice physics

$$\sigma_{0,j} = \frac{\sum_{i=1}^M N_i \sigma_{p,i} + \frac{1/\bar{R}}{1/a + 1/\gamma - 1}}{N_j}$$

- Neglects Dancoff shadowing effect ($\gamma = 1$)
- Neglects empirical correction to the Wigner rational approximation (Bell Factor, $a = 1$)

- **Procedure** for 1G XS generation

- Collapsing of the MG set for different σ_0
- Estimation of the σ_0 value
- The σ_0 value is used to extract the 1G XS

Simplified σ_0 model ($a = \gamma = 1$)



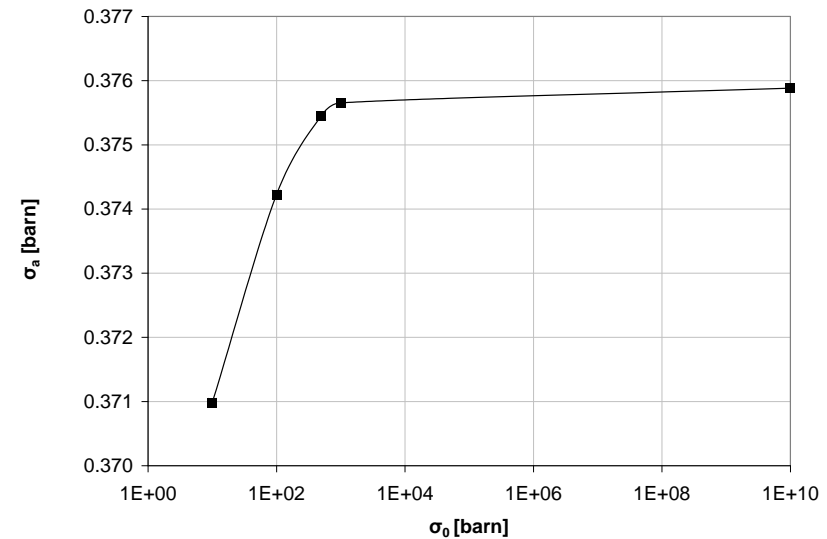
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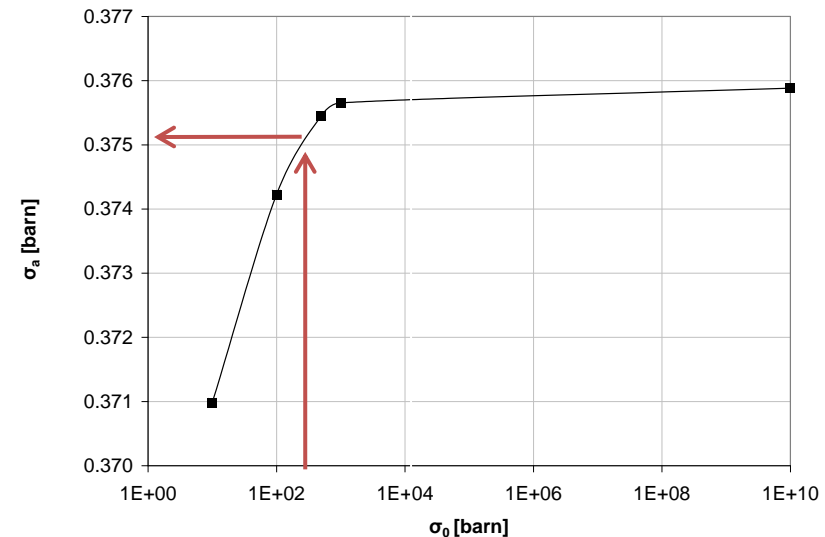
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- In LWRs: $a \sim 1.2$, $\gamma \sim 0.8$

- \Rightarrow cancellation of errors \Rightarrow does not always work





- ☐ How to make MG approach universally applicable?
- ☐ Can it be extended beyond unresolved resonances range?
- ☐ Can the number of groups be reduced?
- ☐ Will this save CPU time?

Reconstruction of σ_0 from MC statistics



- ❑ MCNP collects some RR statistics (table 140)
- ❑ **Can be used to reconstruct σ_0**

$$\sigma_{0,j} = \frac{\sum_{i=1}^M N_i \sigma_{p,i} + \frac{\frac{1/\bar{R}}{1/a + 1/\gamma - 1}}{N_j}}$$

1. Calculate 1G σ_a for nuclide j

2. Collapsing of the MG set for different σ_0

3. Reconstruction of $\sigma_{0,j}$

4. Calculation of R_j^*

5. Calculation of the average

6. The average $\overline{R^*}$ is to calculate the σ_0 and, the 1-g XS for all the nuclides

$$\overline{\sigma_a^j} = \frac{w_c^j + w_f^j \left[\frac{\#}{SN} \right]}{\phi \left[\frac{\#}{cm^2 \cdot SN} \right] \cdot V[cm^3] \cdot N_j \left[\frac{\#}{b \cdot cm} \right]}$$

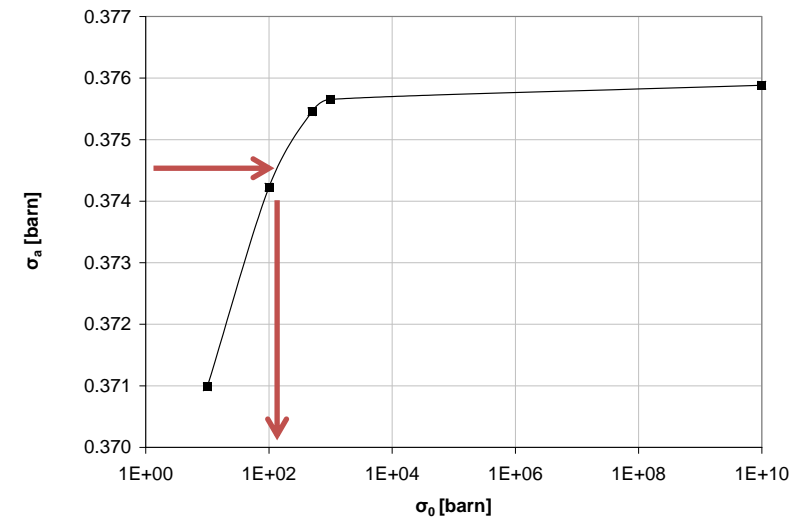
Reconstruction of σ_0 from MC statistics



- MCNP collects some RR statistics (table 140)
- Can be used to reconstruct σ_0

$$\sigma_{0,j} = \frac{\sum_{i=1}^M N_i \sigma_{p,i} + \frac{\frac{1/R}{1/a + 1/\gamma - 1}}{N_j}}$$

1. Calculate of 1-g σ_a for nuclide j
2. Collapse MG set for different σ_0
3. Reconstruct $\sigma_{0,j}$
4. Calculation of R_j^*
5. Calculation of the average $\overline{R^*}$
6. The average $\overline{R^*}$ is to calculate the σ_0 and, the 1-g XS for all the nuclides



Reconstruction of σ_0 from MC statistics



- The model relies on statistical data to calculate (\mathbf{a}, γ)

$$\sigma_{0,j} = \frac{\sum_{i=1}^M N_i \sigma_{p,i} + \frac{1/\bar{R}}{1/a + 1/\gamma - 1}}{N_j}$$

- **Procedure** for 1-g XS generation

1. Calculate of 1-g σ_a for nuclide j

2. Collapse MG set for different σ_0

3. Reconstruct $\sigma_{0,j}$

$$\sigma_{0,j} = \frac{\sum_{i=1}^M N_i \sigma_{p,i} + 1/R_j^*}{N_j}$$

4. Calculation of R_j^*

$$\overline{R^*} = \frac{\sum_{j=1}^M R_j^* \cdot w_a^j}{\sum_{j=1}^M w_a^j}$$

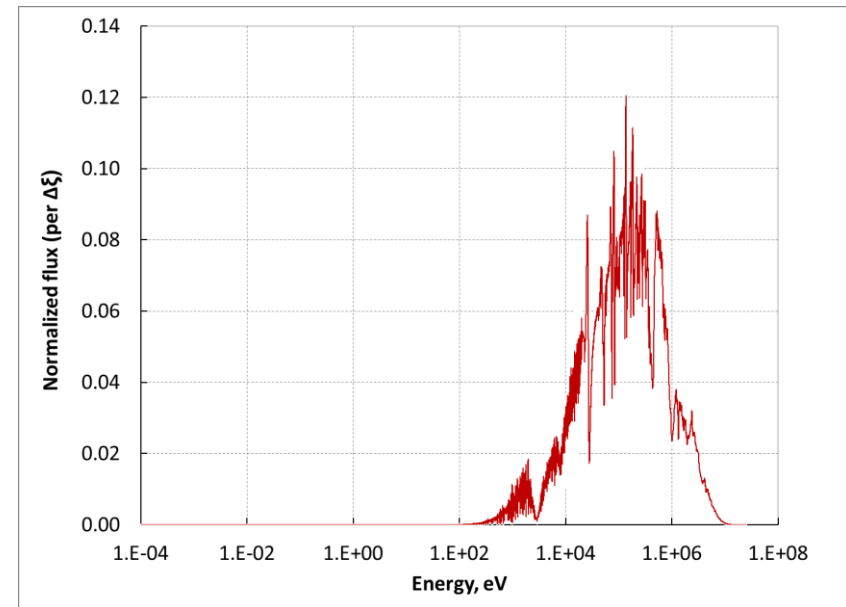
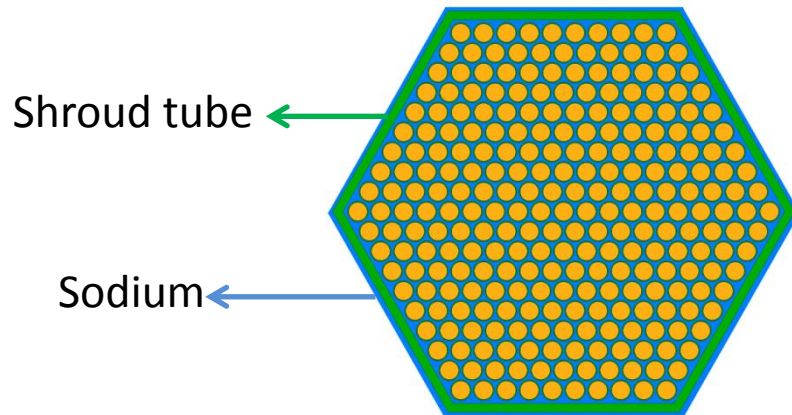
5. Calculation of the average $\overline{R^*}$

6. The average $\overline{R^*}$ is to calculate the σ_0 and 1G XS for all the nuclides

Test case: SFR assembly



- ❑ **Sodium cooled fast reactor (Fiorini and Vasile, 2011)**
 - 38% of total absorption is in unresolved resonances
 - Self-shielding effect is of major importance
- ❑ **Input data**
 - Fuel: Pu MOX
 - Temperature = 300K
 - Power density = 206 W/cm³
 - Number of fuel pins = 271



Results: effect of the XS correction



□ Assembly depletion

- BGCore
- 50,000 energy groups

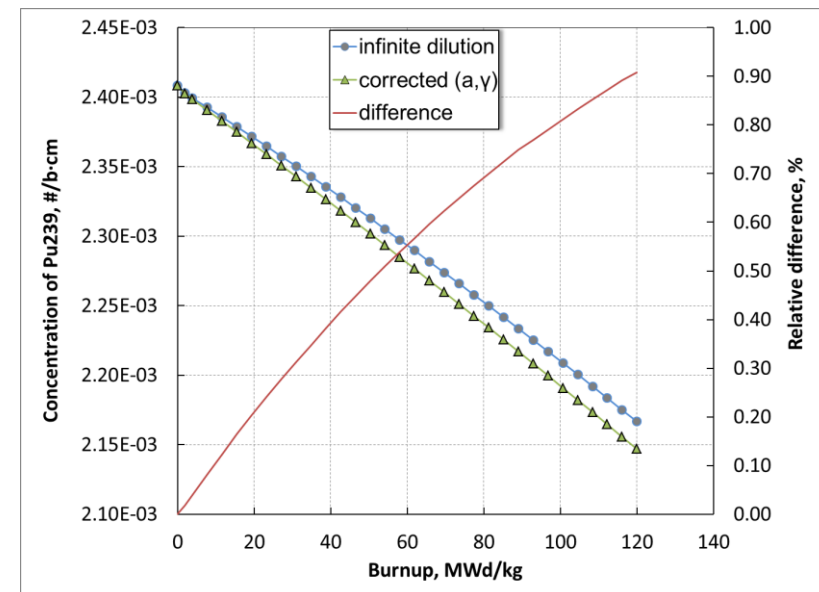
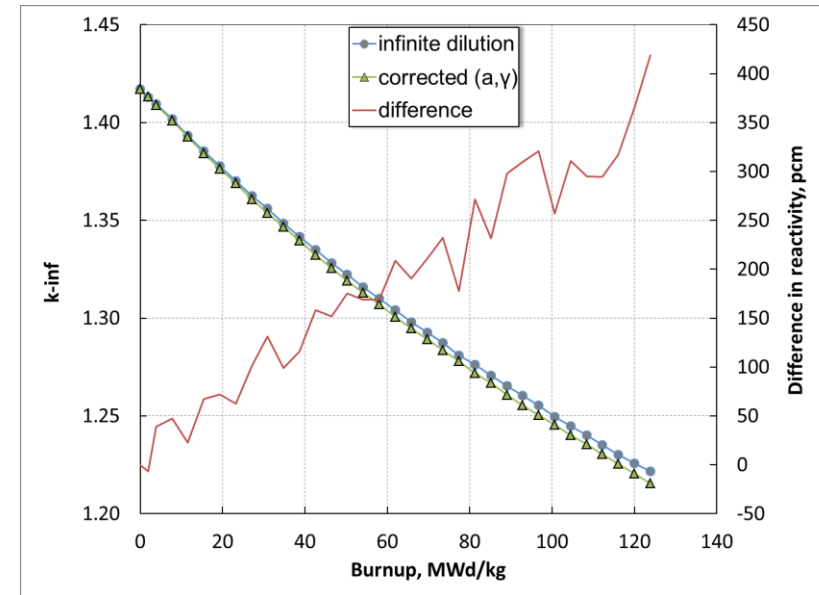
□ Two cases:

1. Infinite dilution cross-sections
2. Self-shielded cross-sections

➤ here: **corrected** (a, γ)

□ Results:

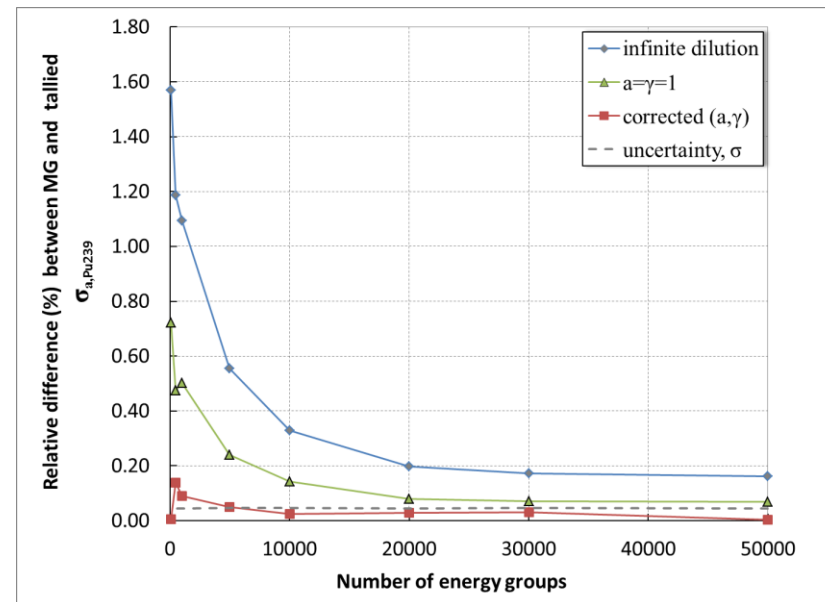
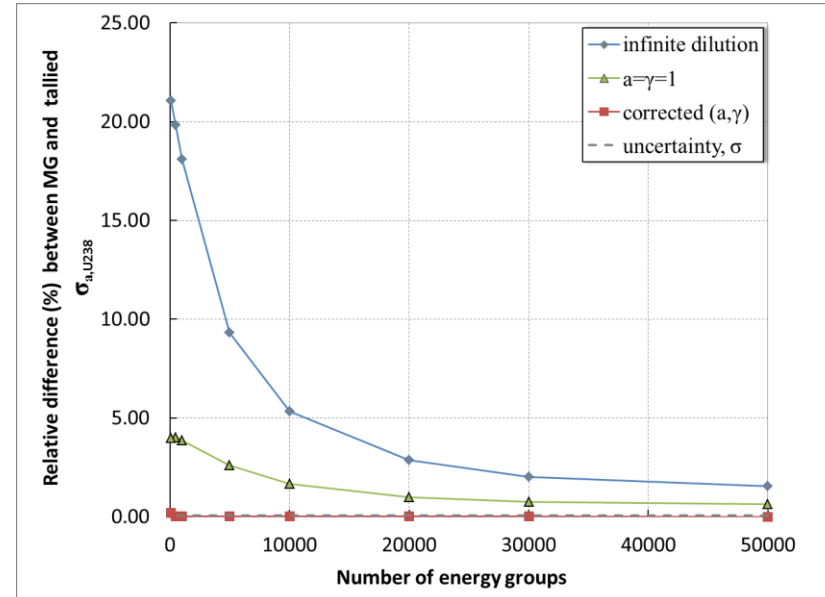
- systematic error in Case 1:
 - 400 pcm in reactivity
 - 1% error in Pu239 concentration
 - Due to the error in 1G XS of U238



Results: No. of energy groups vs. accuracy



- ❑ No depletion
- ❑ Different collapsing methods:
 - Infinite dilution XS
 - Simplified σ_0 model ($a = \gamma = 1$)
 - σ_0 model with corrected a, γ values
- ❑ Reference: direct tally XS
- ❑ 30 independent MC simulations
 - 1G cross sections and statistical uncertainties (1σ)
- ❑ absorption reactions:
 - 39% in U238
 - 38% in Pu239



Storage requirements and CPU time



❑ Memory requirements strongly depends on the #EG

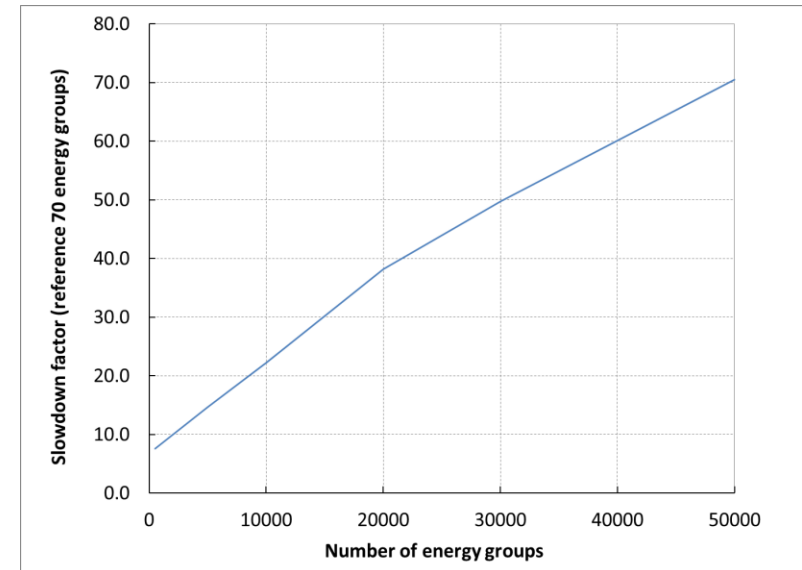
- For a specific nuclide at a specific temperature
 - 70 EG require 27 Kbytes
 - 50,000 EG require 1677 Kbytes
- We need ~340 nuclides at ~10 discrete T
 - 5.7 Gbytes ← 50,000 EG
 - 91 Mbytes ← 70 EG

❑ CPU time for data processing :

- Loading the binary cross section data
- Reading MCNP fluxes

❑ Reducing from 50,000 to 70 EG

- × 70 speed-up





- ❑ Direct tally approach is computationally intensive
- ❑ MG approach is a viable alternative
 - Generate universal MG sets of 1G XS
 - Collapse using fine group MC spectrum
- ❑ MG approach requires extension to be universally applicable
 - Accounting for self shielding requires accurate background XS
 - Background XS can be reconstructed from MC statistics
- ❑ The approach produces accurate shielded 1G XS
 - Even for very small number of energy-groups (e.g. 70)
- ❑ Full core analyses must include multi-zone division and TH
 - Considerable slow down of the overall calculation time



Thank you for your attention